

# Circling An N-Sided Regular Polygon with Straightedge and Compass in Euclidean Geometry

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## Abstract

## Original Research Article

The topic of this article means “one can construct a circle, of which area is equal exactly to a given polygon with  $n$  sides,  $n \in \mathbb{N}$ , using a straightedge and a compass only”. No scientific theory lasts forever, but specific research and discoveries continuously build upon each other. The three classic ancient Greek mathematical challenges likely referring to are “Doubling The Circle”, “Trisecting An Angle” and “Squaring A Circle”, all famously proven Impossible under strict compass-and-straightedge constraints, by Pierre Wantzel (1837) using field theory and algebraic methods [4], then also by Ferdinand von Lindemann (1882) after proving  $\pi$  is transcendental. These original Greek challenges remain impossible under classical rules since their proofs rely on deep algebraic/transcendental properties settled in the 19th century. Recent claims may involve reinterpretations or unrelated advances but do overturn the conclusions above. Among these, the “Squaring A Circle” problem and related problems involving  $\pi$  have captivated both professional and amateur mathematicians for millennia. The title of this paper refers to the concept of “constructing a circle that has the exact area of a given polygon with  $n$  sides,  $n \in \mathbb{N}$ ,” or “Circling A Regular Polygon” for short. The circling is similar to research idea arose after the “Circling A Square” problem was studied and solved and published in “Scholars Journal of Physics, Mathematics and Statistics” in 2024 [7]. This paper presents an exact solution to constructing a circle, that is concentric with and has the same area as a given polygon with  $n$  sides. The solution does not rely on the number  $\pi$  and adheres strictly to the constraints of Euclidean Geometry, using only a straightedge and compass. The technique of “ANALYSIS” is employed to solve the “Circling A Regular Polygon” problem precisely and exactly with only a straightedge and compass, without altering any premise of the problem. This independent research demonstrates the solution to the challenge using only these tools. All mathematical tools and propositions in this solution are derived from Euclidean geometry. The methodology involves geometric methods to arrange the given polygon with  $n$  sides, and its equal-area circle (assumed existing) into a concentric position.

**Keywords:** Circling polygon; circle and regular polygon; circle polygon; polygon area of a circle; constructing a circle with the same area as a polygon; Euclidean geometry; straightedge and compass.

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## 1. INTRODUCTION

For over three millennia, three well-known classical geometric problems from ancient Greece Squaring the Circle, Doubling the Cube, and Trisecting an Angle emerged and challenged the ingenuity of mathematicians. These problems, first posed by the constraint of using only an unmarked straightedge and compass, have long been declared impossible to solve within the framework of Euclidean geometry. Foundational impossibility proofs by 19th-century mathematicians, such as Pierre Wantzel and Ferdinand Von Lindemann [2], [3], and [4], - using algebraic field theory and transcendental number theory, - seem to confirm that exact solutions are unattainable.

Specifically, the transcendence of  $\pi$  implies that a square with an area exactly equal to that of a given circle cannot be constructed using purely geometric means [2] and [3]. However, while these algebraic impossibility theorems are rigorous within their own domains, they diverge in nature from the original geometric spirit of ancient challenges. The historical emphasis on purely constructive geometry, devoid of algebra, arithmetic, or trigonometry, leaves space for critical re-evaluation [6].

*Among them, Hippocrates meticulously studied the problem of squaring the circle. The problem is stated as follows: Using only a straightedge and a compass, is it possible to construct a square with an area equal to a*

given circle? The problems were proven unsolvable using only straightedge and compass in the 19th century. In 1882, mathematician Ferdinand von Lindemann proved that  $\pi$  is an irrational number, which means that it is impossible to construct a square with the same area as a given circle using only a straightedge and a compass, as posed by Hippocrates. One of the most fascinating aspects of this problem is that it has captured the interest of mathematicians throughout the history of mathematics. From the earliest mathematical documents to today's mathematics, the problem and its relation to  $\pi$  have intrigued both professional and amateur mathematicians for millennia.

A significant step forward in proving the impossibility of squaring the circle occurred in 1761 when Lambert proved that  $\pi$  is irrational [2] & [3]. This, however, was not sufficient to demonstrate the impossibility of squaring the circle using a straightedge and compass, as certain algebraic numbers can be constructed with these tools. Despite the proof of the impossibility of squaring the circle, the problem has continued to captivate mathematicians and the general public alike, remaining an important topic in the history and philosophy of mathematics.

In 1837, French mathematician L. Wantzel proved that the three classical problems of ancient Greece are impossible to solve using only a straightedge and compass. Although based on algebra, Pierre Laurent Wantzel (1837) declared the verdict, "Arbitrary angle trisection is impossible", I experienced that my achieved procedure was possibly not arrested by this verdict [4]. After applying my method to trisect an arbitrary angle, I hope readers can trust algebra cannot affect the successful geometrical constructions of angle trisection.

Therefore, the problems of squaring the circle, doubling the cube, and trisecting an angle have been studied for centuries and remain unsolvable with these tools to this day. As of December 2022, no mathematician has found exact solutions to classical problems such as "Doubling the Cube," "Squaring the Circle," and "Trisecting an Angle" using only a compass and straightedge.

However, in 2023, my research article, published on the SJPMS journal, [6] as an exact solution to the "Squaring the Circle" problem, provides a counter-proof to the impossibility stated by Wantzel in 1837, [4].

This article arises from such a re-evaluation and documents a new geometric approach remaining strictly within the constraints of compass and straightedge that aims to construct precise solutions to several of these age-old problems. Beginning with a geometric interpretation of Lao Tzu's aphorism "The Great Way is simple," the author explores the power of simplicity and

concentric arrangement. Through detailed analysis, an exact method for Squaring the Circle was developed, followed by solutions for Doubling the Cube and Trisecting an Angle, each derived using geometric reasoning alone in 2023, 2024, and 2025 [6], [8], and [9].

In the past, knowledge was often considered scientific if it could be confirmed through specific evidence or experimentations. However, Karl Popper, in his book *Logik der Forschung* (The Logic of Scientific Discovery) published in 1934, demonstrated that a fundamental characteristic of scientific hypotheses is their ability to be proven wrong (falsifiability). Anything that cannot be refuted by evidence is temporarily regarded as true until new evidence emerges. For instance, in astronomy, the Big Bang theory is widely accepted; however in the future, anyone who discovers a flaw in this theory will be acknowledged by the entire physics community. Furthermore, no scientific theory lasts forever; rather, it is specific research and discoveries that continually build upon one another [1].

Starting from accepted premises, without proof, one uses deductive reasoning to arrive at theorems and corollaries. With different premises, we develop different mathematical systems. For example, the premise "from a point outside a line, only one parallel line can be drawn to the given line" leads to Euclidean geometry. If we assume that no parallel lines can be drawn from that point, we enter the realm of Riemannian geometry. Alternatively, Lobachevskian geometry assumes that an infinite number of parallel lines can be drawn through that point.

It is important to clarify that this does not imply that a square with an area equal to a circle does not exist. If the circle has area  $A$ , a square with a side length equal to the square root of  $A$  would have the same area. This does not imply that it is impossible to solve the problem using only a straightedge and a compass. Thus, I provided the exact solution to the "Squaring the Circle" problem without altering the premises of Euclidean geometry or the constraints of straightedge and compass [6]. In 2024, I also solved the inverse problem, titled "Circling A Square With Straightedge & Compass in Euclidean Geometry," which was published in the SJPMS [7].

The above topic "Circling An  $n$ -Sided Regular Polygon With Straightedge And Compass In Euclidean Geometry" refers to the process of "constructing a circle that has the same area as a given regular polygon with  $n$  sides,  $n \in \mathbb{N}$ , and is concentric with that polygon." This concept came to me spontaneously after solving the problem of "Circling The Circle." I thought, "If one can circle the square, can one also circle a regular polygon using only a straightedge and compass in Euclidean Geometry?" In other words, "Circling A Regular Polygon" is a new challenge problem that arose from the exact solution presented in

my “Circling A Square” paper published in *SJPMS* [7]. Therefore, the “*Circling A Regular Polygon With  $n$  Sides*” challenge and its solution did not exist in the field of mathematics until it was solved and published by this paper.

In seeking solutions to such problems, geometers developed a special technique called “ANALYSIS.” They assumed that the problem had been solved, and by investigating the properties of the solution, they worked backward to identify an equivalent problem that could be solved based on the given conditions.

To obtain a formally correct solution to the original problem, geometers reverse the process, starting with the data to solve the equivalent problem derived through analysis, and then use that solution to solve the original problem.

This reverse procedure is known as “SYNTHESIS.” Analysis and synthesis are fundamental methods for mathematical reasoning and problem-solving. Analysis involves breaking down complex mathematical problems or structures into simpler and more manageable components. It enables mathematicians to understand the underlying principles, identify patterns, and isolate essential variables. Through analytical methods, one can derive conclusions, test hypotheses, and explore the logical consequences of these assumptions.

Conversely, synthesis entails the combination of previously understood elements to construct more complex systems or develop general theories. It often follows analysis, using the insights gained to build new models, solve broader problems, or formulate proofs. The interplay between analysis and synthesis fosters deeper comprehension of mathematical concepts and drives the progression of mathematical theory.

Together, these complementary approaches are vital to the advancement of mathematics, underpinning both theoretical inquiry and practical applications.

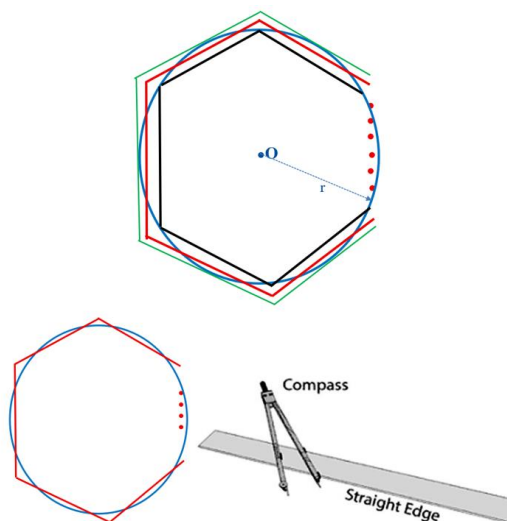
I have adopted both “ANALYSIS” and “SYNTHESIS” techniques to solve this “Circling A Regular Polygon” problem exactly, using only a straightedge, compass, in Euclidean Geometry, without involving the irrational number  $\pi$ .

The inspiration for this research arose after the solution to the “Circling A Square” problem was published in *SJPMS* in 2024 [7]. If it is possible to circle a square using Euclidean geometry, *why is it difficult to circle a regularly polygon?*

In this context, the given polygon contains an inscribed regular polygon with  $2n$  sides,  $n \in \mathbb{N}$  where the radius of the polygon with  $2n$  sides is the radius of the resulting circle. This *Resulting Circle* serves as the solution to the new problem of “Circling A Regular Polygon,” as required. The remaining task is to prove that the area of the resulting circle is equal to the area of the given polygon with  $n$  sides. This paper also introduces a new mathematical tool, the “Regular  $2n$ -Sided Polygon Ruler,” and provides a proof for the following:

1. a circle intersects the given polygon with  $n$  sides at the  $2n$  vertices of a special polygon;
2. the construction process forms a circle with radius equal to the radius of the regular polygon with  $2n$  sides inscribed in the given polygon with  $n$  sides.

*This paper’s solution to the “Circling A Regular Polygon With  $n$  Sides” problem is naturally ended up the process from solutions to “Circling Regular Triangle”, “Circling A Squaring”, “Circling A Regular Pentagon”, “Circling A Regular Hexagon”, ..., “Circling A Regular Polygon” problems.*

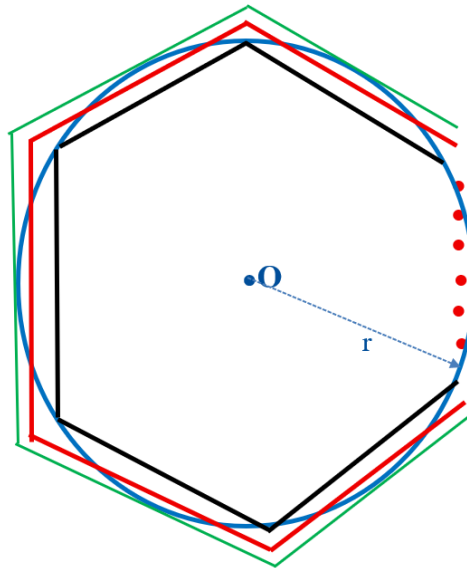


# I. PROOFS OF NEW PROPOSITIONS

## I.1 Theorem 1:

If there exists a circle  $(O, r)$  [regular polygon with  $n$  sides,  $n \in \mathbb{N}$ ,] that has the same area as a given

regular polygon with  $n$  sides,  $n \in \mathbb{N}$ , then circle  $(O, r)$  cuts the polygon at  $2n$  points to form an inscribed polygon with  $2n$  sides in the circle.



**Figure 1:** Red polygon is the given regular polygon, and the circle (blue color) assuming to have the same area as area of the given polygon. The black polygon is inscribed in the circle & the green polygon is the circumscribed polygon of the circle. They are all concentric to the given polygon center and have parallel sides.

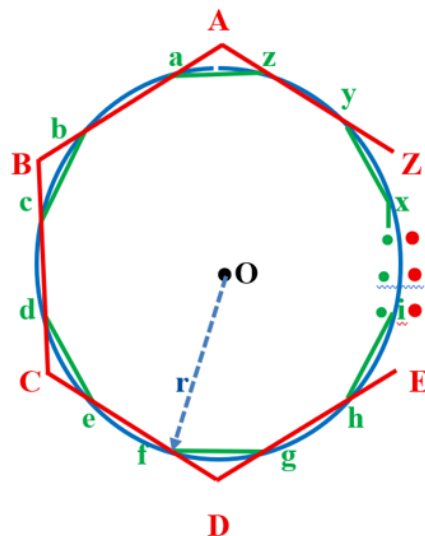
## PROOF:

Assuming that the blue circle  $(O, r)$  in Figure 1 is a resulting shape that has the same area as the area of a given red polygon with  $n$  sides and concentrated with the given polygon, then

- The area of this circle  $(O, r)$  is less than the area of the circumscribed regular polygon (green) of the circle.
- The area of this blue circle  $(O, r)$  is larger than

the area of the inscribed regular polygon (black) in the circle.

Thus, this blue circle  $(O, r)$  has to cut the  $n$  sides of the given polygon  $2n$  points  $a, b, c, d, e, f, g, h, i, \dots, x, y, z$  (figure below). These  $2n$  points are vertices of an inscribed polygon with  $2n$  sides in the resulting circle  $(O, r)$ , as required and described in Figure 2 below.



**Figure 2:** The given red polygon ABCDE...Z with  $n$  sides and the inscribed regular polygon abcdefghi...xyz with  $2n$  sides in the blue resulting circle  $(O, r)$ .

## I.2 Theorem 2:

Assume that there exists a circle (O, r), which has the same area as a given regular polygon ABCDE...YZ, then the polygon cuts the circumference of the circle (O, r) at 2n points a, b, c, d, e, f, g, h, i, ..., x, y & z, which are 2n vertices of an inscribed regular polygon of the given circle.

### PROOF:

Let the regular polygon ABCDE...YZ in Figure 3 be given; then, assume that there exists a circle (O, r) – blue color, - which has the same area as the area of the regular polygon ABCDE...YZ, and is concentric to the polygon.

According to Theorem 1 in section I.1 above, n sides of this polygon cut the circumference of the circle at 2n points a, b, c, d, e, f, g, ..., x, y & z (Figure 3, below). Let circle (O, R) be the circumscribed circle of the regular polygon ABCD...YZ.

Extend chord ab (Figure 3 below) of the circle (O, r) to meet the circumference of the circle (O, R) at points A' & B', and then connect the center points O to A'. From point A', draw a symmetric straight line segment A' Z' (the black arrow line in Figure 3), which

Line OA' is the bisector of angle B'A'Z'. Because of the symmetrical property of lines A' B' and A'Z' and circle chords ab & yz (Figure 3 below), line A'Z' overlaps the chord yz of the circle (O, r). Similar extensions of chords cd, ef, g..., & ...x and connections B'O, C'O, D'O, ... & Z'O and the similar symmetric proofs above show that A'B'C'D'...Z' is also an inscribed regular polygon with n sides in the circle (O, R).

Therefore, these two regular polygons are equal, and their intersect area is polygon abcdefg...xyz, - with 2n sides - (Figure 3 below), which is a regular inscribed polygon with 2n sides in the given circle (O, r). This shows that the side extensions of this 2n polygon intersect exactly at n vertices of the required regular polygon ABCD...YZ and n vertices of polygon A'B'C'D'...Z', equally (Figure 3).

By the symmetric and concentric properties of these 2 polygons,

$$\text{Polygon ABCD...YZ} = \text{Polygon A'B'C'D'...Z'} \quad (1)$$

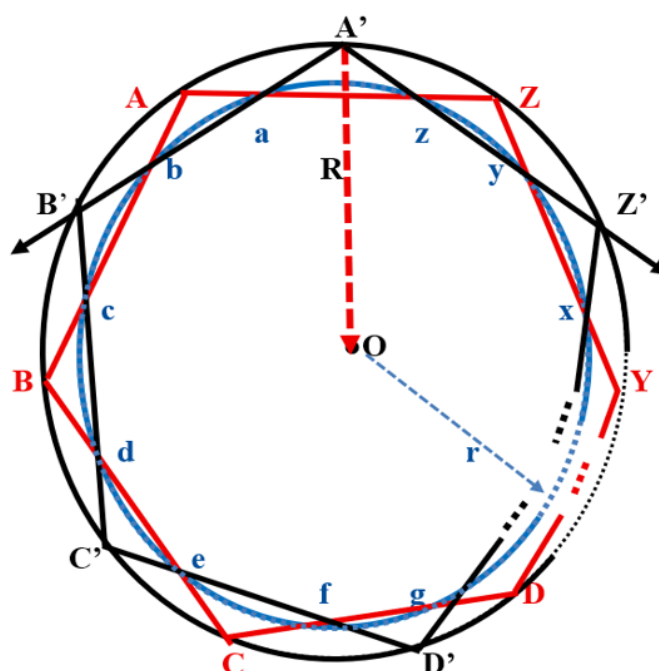


Figure 3: The given circle (O, r) – blue color -, the regular polygon ABCD...YZ with n sides and the regular A'B'C'D'...Z' with n sides.

Because (O, r) and (O, R) are two concentric circles, symmetric properties, and equal distances from the center O to 2n chords ab, bc, cd, de, ef, fg, g..., ...x, xy, yz and za, and abcdefg...xyz is a regular polygon with 2n sides as follows:

$$ab = bc = cd = de = ef = fg = g... = ...x = xy = yz = za \quad (2)$$

From (2), the inscribed polygon abcdefg...xyz of the given circle (O, r) is an identification of the resulting circle (O, r) itself, as required (Figure 3).

### I.3 DEFINITION:

According to Theorem 2 in Section I.2 above, let  $n \in \mathbb{N}$ , and the given regular polygon ABCD...YZ, then a resulting circle (O, r), area =  $\pi r^2$ , then any regular

polygon with  $2n$  sides inscribed in the circle and the polygon is defined as "CIRCLING POLYGON

RULER" (Figure 4 below).

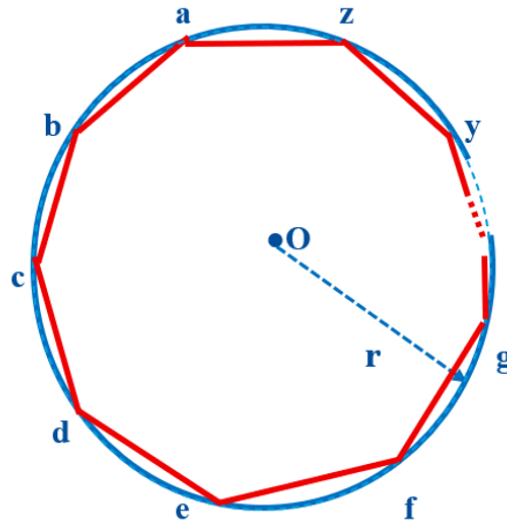


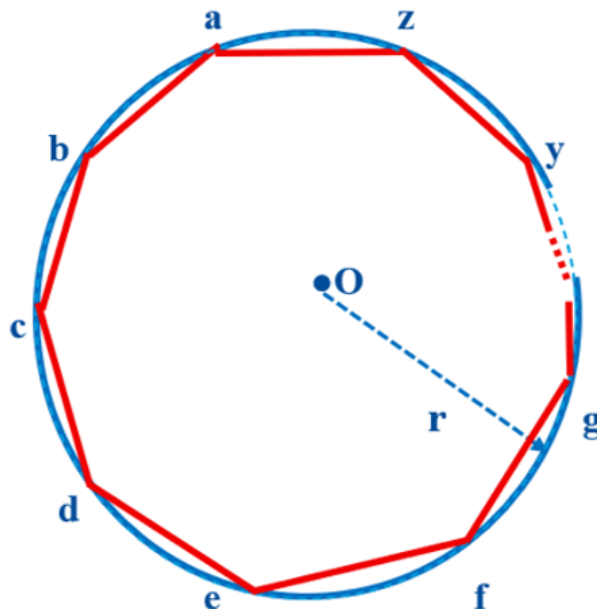
Figure 4: The extracted Circle  $(O, r)$  and regular polygon  $abcdeg...yz$  with  $2n$  sided for the above definition of a "Circling Polygon Ruler.

## II. CORE THEOREM CORE THEOREM

Let a regular polygon with  $n$  sides,  $n \in \mathbb{N}$ , be given, then a CIRCLE POLYGON RULER with  $2n$  sides within the polygon is a mathematics tool for constructing a circle  $(O, r)$ , which has the same area as the area of the given polygon, using only a straightedge & compass in Euclidean Geometry.

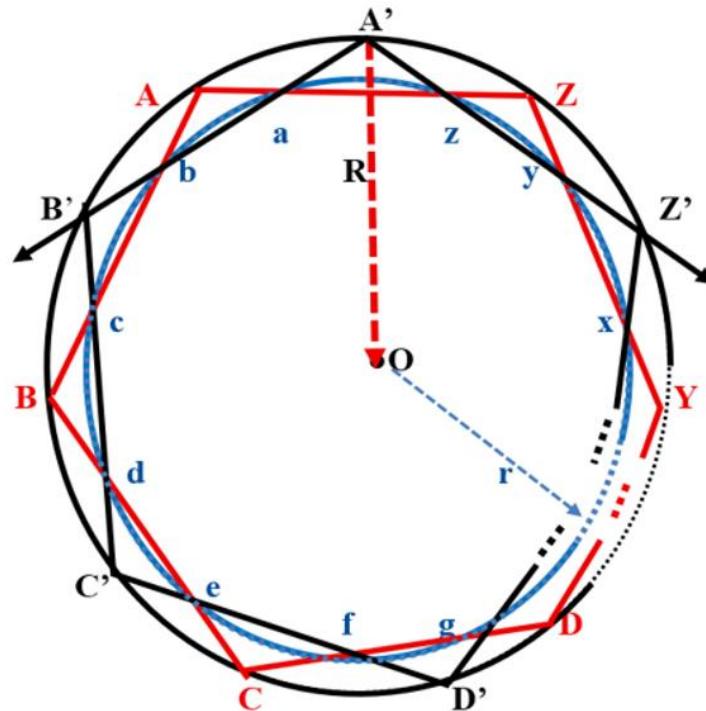
## PROOF:

Given a regular polygon with  $n$  sides,  $n \in \mathbb{N}$ , then by Theorem 1 in Section I.1, Theorem 2 in Section I.2 and Definition in Section I.3 above, there exists a regular polygon  $abcdeg...xyz$  with  $2n$  sides, inscribed in the resulting circle  $(O, r)$ , which is the Circling Polygon Ruler, as shown in the following figure.



Extend  $2n$  sides  $ab, bc, de, fg, \dots, xy, yz$  and  $za$  of the Circling Polygon Ruler  $abcdeg...yz$  to obtain the given  $ABCD...YZ$  (red color in Figure 5) and an equal

regular polygon  $A'B'C'D'...Z'$ . These two polygons intersect at all vertices of the Circling Polygon Ruler (Figure 5).



**Figure 5: The regular polygon abcdefg...xyz with  $2n$  sides (blue colour) inscribed in the resulting circle  $(O, r)$  and the given polygon ABCD...YZ of the “Circling A Polygon” challenge problem.**

### III. DISCUSSION AND CONCLUSION

Can mathematicians use a compass and a straightedge to construct a circle of equal area to a given regular polygon with  $n$  sides, using only a straightedge and compass? The results of my independent research successfully get an exact solution to a deduced /derivative problem “Circling A Square” of the ancient Greek “Squaring A Circle” problem challenge showing the idea that “If one can solve “circling a square” then one can also solve the general problem “circling a regular polygon of  $n$  sides,  $n \in \mathbb{N}$ ” too ...

This study proves that it is certain to construct a circle  $(O, r)$ , which has the same area  $\pi r^2$  as the area of a given regular polygon with  $n$  sides, successfully with only straightedge and compass in Euclidean Geometry.

In addition, this circle  $(O, r)$  has the same area  $\pi r^2$  as the area  $A$  of the given polygon with  $n$  sides. My solutions to the “Squaring A Circle” and “Circling A Square” problems, published on the SJPMs on 31/10/2024 [6] and [7].

This construction method is quite different from the approximation and is based on using only a straightedge and compass within Euclidean Geometry.

*The inspiration for this research arose after the solution to the “Squaring The Circle” and “Circling A Square” problems was published in SJPMs in 2024 [6] and [7]. If it is possible to circle a square using only a straightedge and compass in Euclidean geometry, then a question arises: why is it difficult to circle a given*

*regular polygon with  $n$  sides, similar to how one circles a given square?*

*In this context, the given polygon with  $n$  sides contains an inscribed regular polygon having  $2n$  sides, which serves as a “circling polygon ruler” inscribed in the target circle  $(O, r)$ .*

*The radius  $r$  of this circle serves as the solution to construct  $(O, r)$ , using straightedge and compass. The remaining task is to prove that the area of this circle is exactly equal to the area of the given polygon with  $n$  sides. This paper also introduces a new mathematical tool, called the “Circling Polygon Ruler,” and provides a proof for the following statements:*

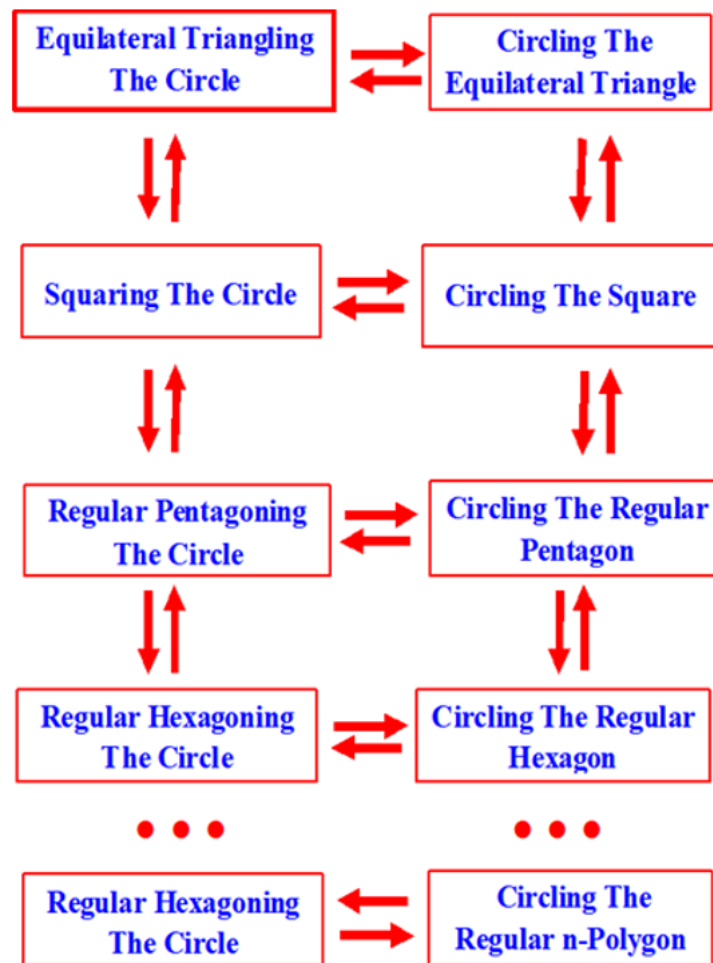
- (1) A concentric circle intersects the given regular polygon with  $n$  sides at  $2n$  vertices and forms a special polygon with  $2n$  side, and with two non-consecutive sides symmetrically positioned;**
- (2) This solution construction forms a Circling Polygon Ruler ( $2n$  sides) inscribed in the resulting circle.**

This method of exact “Circling A Regular Polygon” above, is deduced, conversely, from another method of the new mathematical challenge “Regular Polygonising A Circle” with a straightedge and a compass only, in Euclidean Geometry, published in IJPMS journal on 24/07/2026 [21]. In detail, we summarize this as follows,

*Given a regular polygon with  $n$  sides  $a$  and area  $A$ ,  $a, A \in \mathbb{R}$ , then use a straightedge & a compass to*

construct an accurate circle, which has the exact area  $A$ . The, how to solve this new geometry problem is described in Section I above, to obtain a circle without using the traditional constant  $\pi$ .

Finally, derivatives from the “Squaring A Circle” problem (ancient Greek challenge) can be described in the following diagram:



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